

# Funzioni principali del Matlab

**BODE** Bode frequency response of LTI systems.

`BODE(SYS)` draws the Bode plot of the LTI system `SYS`. The frequency range and number of points are chosen automatically.

`BODE(SYS,{WMIN,WMAX})` draws the Bode plot for frequencies between `WMIN` and `WMAX` (in radian/second).

`BODE(SYS,W)` uses the user-supplied vector `W` of frequencies, in radian/second, at which the Bode response is to be evaluated. See `LOGSPACE` to generate logarithmically spaced frequency vectors.

`BODE(SYS1,SYS2,...,W)` plots the Bode response of multiple LTI systems `SYS1,SYS2,...` on a single plot. The frequency vector `W` is optional. You can also specify a color, line style, and marker for each system, as in `bode(sys1,'r',sys2,'y--',sys3,'gx')`.

When invoked with left-hand arguments,

`[MAG,PHASE,W] = BODE(SYS,...)` returns the frequency vector `W` and arrays `MAG` and `PHASE` of magnitudes (in dB) and phases (in degrees). No plot is drawn on the screen. If `SYS` has `NU` inputs and `NY` outputs and `LW=length(W)`, `MAG` and `PHASE` are `NY-by-NU-by-LW` arrays and the response at the frequency `W(k)` is given by `MAG(:, :, k)` and `PHASE(:, :, k)`.

For discrete systems with sample time `Ts`, `BODE` uses the transformation  $Z = \exp(j*W*Ts)$  to map the unit circle to the real frequency axis. The frequency response is only plotted for frequencies smaller than the Nyquist frequency  $\pi/Ts$ , and the default value 1 (second) is assumed when `Ts` is unspecified.

**CTRB** Form the controllability matrix.

`CO = CTRB(A,B)` returns the controllability matrix  $[B \ AB \ A^2B \ \dots]$ .

`CO = CTRB(SYS)` returns the controllability matrix of the state-space system `SYS` with realization  $(A,B,C,D)$ . This is equivalent to `CTRB(sys.a,sys.b)`

**DAMP** Natural frequency and damping factor of LTI system poles.

`[Wn,Z] = DAMP(SYS)` returns vectors `Wn` and `Z` containing the

natural frequencies and damping factors of the LTI system SYS. For discrete-time systems, the equivalent s-plane natural frequency and damping ratio of an eigenvalue lambda are given by:

$$W_n = \text{abs}(\log(\text{lamba}))/T_s, \quad Z = -\cos(\text{angle}(\log(\text{lamba})))$$

Wn and Z are empty vectors if the sample time Ts is undefined.

[Wn,Z,P] = DAMP(SYS) also returns the system poles P.

When invoked without left-hand arguments, DAMP prints the poles with their natural frequency and damping factor in a tabular format on the screen. The poles are sorted by increasing frequency.

**DCGAIN** DC gain of LTI systems.

K = DCGAIN(SYS) computes the steady state (D.C. or low frequency) gain of the system SYS.

**ESORT** Sort complex continuous eigenvalues in descending order.

S = ESORT(P) sorts the complex eigenvalues in the vector P in descending order by real part. The unstable eigenvalues (in the continuous-time sense) will appear first.

[S,NDX] = ESORT(P) also returns the vector NDX containing the indexes used in the sort.

**IMPULSE** Impulse response of LTI systems.

IMPULSE(SYS) plots the impulse response of each input channel of the LTI system SYS. The time range and number of points are chosen automatically. The infinite pulse at  $t = 0$  in the response of continuous systems with direct feedthrough is disregarded.

IMPULSE(SYS,TFINAL) simulates the impulse response from  $t = 0$  to the final time  $t = \text{TFINAL}$ . For discrete-time systems with unspecified sampling time, TFINAL is interpreted as the number of samples.

IMPULSE(SYS,T) uses the user-supplied time vector T for simulation. For discrete-time systems, T should be of the form  $T_i:T_s:T_f$  where  $T_s$  is the sample time of the system. For continuous systems, T should be of the form  $T_i:dt:T_f$  where dt will become the sample time of a discrete approximation to the continuous system.

`IMPULSE(SYS1,SYS2,...,T)` plots the step response of multiple LTI systems `SYS1,SYS2,...` on a single plot. The time vector `T` is optional. You can also specify a color, line style, and marker for each system, as in `impulse(sys1,'r',sys2,'y--',sys3,'gx')`.

When invoked with left-hand arguments,

`[Y,T] = IMPULSE(SYS, ...)`

returns the output response `Y` and the time vector `T` used for simulation. No plot is drawn on the screen. If `SYS` has `NU` inputs and `NY` outputs, and `LT=length(T)`, the array `Y` is `LT-by-NY-by-NU` and `Y(:,j)` gives the impulse response of the `j`-th input channel.

For state-space systems,

`[Y,T,X] = IMPULSE(SYS, ...)`

also returns the state trajectory `X` which is an `LT-by-NX-by-NU` array if `SYS` has `NX` states.

## **INITIAL** Initial condition response of state-space models.

`INITIAL(SYS,X0)` plots the undriven response of the state-space system `SYS` with initial condition `X0` on the states. This response is characterized by the equations

Continuous time:  $\dot{x} = A x, y = C x, x(0) = x_0$

Discrete time:  $x[k+1] = A x[k], y[k] = C x[k], x[0] = x_0$ .

The time range and number of points are chosen automatically.

`INITIAL(SYS,X0,TFINAL)` simulates the time response from  $t = 0$  to the final time  $t = \text{TFINAL}$ . For discrete-time systems with unspecified sample time, `TFINAL` should be the number of samples.

`INITIAL(SYS,X0,T)` specifies a time vector `T` to be used for simulation. For discrete systems, `T` should be of the form `0:Ts:Tf` where `Ts` is the sample time of the system. For continuous systems, `T` should be of the form `0:dt:Tf` where `dt` will become the sample time of a discrete approximation of the continuous system.

`INITIAL(SYS1,SYS2,...,X0,T)` plots the response of multiple LTI systems `SYS1,SYS2,...` on a single plot. The time vector `T` is optional. You can also specify a color, line style, and marker for each system, as in `initial(sys1,'r',sys2,'y--',sys3,'gx',x0)`.

When invoked with left hand arguments,

`[Y,T,X] = INITIAL(SYS,X0,...)`

returns the output response  $Y$ , the time vector  $T$  used for simulation, and the state trajectories  $X$ . No plot is drawn on the screen. The matrix  $Y$  has  $\text{LENGTH}(T)$  rows and as many columns as outputs in  $\text{SYS}$ . Similarly,  $X$  has  $\text{LENGTH}(T)$  rows and as many columns as states.

**LSIM** Simulation of the time response of LTI systems to arbitrary inputs.

$\text{LSIM}(\text{SYS},U,T)$  plots the time response of the LTI system  $\text{SYS}$  to the input signal described by  $U$  and  $T$ . The time vector  $T$  consists of regularly spaced time samples and  $U$  is a matrix with as many columns as inputs and whose  $i$ -th row specifies the input value at time  $T(i)$ .

For instance,

```
t = 0:0.01:5; u = sin(t); lsim(sys,u,t)
```

simulates the response of  $\text{SYS}$  to  $u(t) = \sin(t)$  during 5 seconds.

In discrete time,  $U$  should be sampled at the same rate as the system ( $T$  is then redundant and can be omitted or set to the empty matrix). In continuous time, the sampling period  $T(2)-T(1)$  should be chosen small enough to capture the details of the input signal. The time vector  $T$  is resampled when intersample oscillations may occur.

$\text{LSIM}(\text{SYS},U,T,X0)$  specifies an additional nonzero initial state  $X0$  (for state-space systems only).

$\text{LSIM}(\text{SYS1},\text{SYS2},\dots,U,T,X0)$  simulates the response of multiple LTI systems  $\text{SYS1},\text{SYS2},\dots$  on a single plot. The initial condition  $X0$  is optional. You can also specify a color, line style, and marker for each system, as in `lsim(sys1,'r',sys2,'y--',sys3,'gx',u,t)`.

When invoked with left hand arguments,

```
[Y,T] = LSIM(SYS,U,...)
```

returns the output history  $Y$  and time vector  $T$  used for simulation. No plot is drawn on the screen. The matrix  $Y$  has  $\text{LENGTH}(T)$  rows and as many columns as outputs in  $\text{SYS}$ .

For state-space systems,

```
[Y,T,X] = LSIM(SYS,U,...)
```

also returns the state trajectory  $X$ , a matrix with  $\text{LENGTH}(T)$  rows and as many columns as states.

**OBSV** Form the observability matrix.

$\text{OB} = \text{OBSV}(A,C)$  returns the observability matrix  $[C; CA; CA^2 \dots]$

$\text{CO} = \text{OBSV}(\text{SYS})$  returns the observability matrix of the state-space system  $\text{SYS}$  with realization  $(A,B,C,D)$ . This is equivalent to

**OBSV**(sys.a,sys.c)

**RANK** Matrix rank.

**RANK**(A) provides an estimate of the number of linearly independent rows or columns of a matrix A.

**RANK**(A,tol) is the number of singular values of A that are larger than tol.

**RANK**(A) uses the default  $\text{tol} = \max(\text{size}(A)) * \text{norm}(A) * \text{eps}$ .

**REAL** Complex real part.

**REAL**(X) is the real part of X.

See I or J to enter complex numbers.

**SS2ZP** State-space to zero-pole conversion.

**[Z,P,K] = SS2ZP(A,B,C,D,IU)** calculates the transfer function in factored form:

$$H(s) = C(sI-A)^{-1} B + D = k \frac{(s-z_1)(s-z_2)\dots(s-z_n)}{(s-p_1)(s-p_2)\dots(s-p_n)}$$

of the system:

$$\begin{aligned} \dot{x} &= Ax + Bu \\ y &= Cx + Du \end{aligned}$$

from the single input IU. The vector P contains the pole locations of the denominator of the transfer function. The numerator zeros are returned in the columns of matrix Z with as many columns as there are outputs y. The gains for each numerator transfer function are returned in column vector K.

**STEP** Step response of LTI systems.

**STEP**(SYS) plots the step response of each input channel of the LTI system SYS. The time range and number of points are chosen automatically.

**STEP**(SYS,TFINAL) simulates the step response from  $t = 0$  to the final time  $t = \text{TFINAL}$ . For discrete-time systems with unspecified sampling time, TFINAL is interpreted as the number of samples.

**STEP**(SYS,T) uses the user-supplied time vector T for simulation. For discrete-time systems, T should be of the form  $T_i:T_s:T_f$  where  $T_s$  is the sample time of the system. For continuous systems,

T should be of the form  $T_i:dt:T_f$  where dt will become the sample time of a discrete approximation to the continuous system.

`STEP(SYS1,SYS2,...,T)` plots the step response of multiple LTI systems `SYS1,SYS2,...` on a single plot. The time vector `T` is optional. You can also specify a color, line style, and marker for each system, as in `step(sys1,'r',sys2,'y--',sys3,'gx')`.

When invoked with left-hand arguments,

`[Y,T] = STEP(SYS,...)`

returns the output response `Y` and the time vector `T` used for simulation. No plot is drawn on the screen. If `SYS` has `NU` inputs and `NY` outputs, and `LT=length(T)`, the array `Y` is `LT-by-NY-by-NU` and `Y(:,j)` gives the step response of the `j`-th input channel.

For state-space systems,

`[Y,T,X] = STEP(SYS,...)`

also returns the state trajectory `X` which is an `LT-by-NX-by-NU` array if `SYS` has `NX` states.

**TF** Specify transfer functions or convert LTI model to transfer function.

`TFSYS = TF(SYS)` converts an arbitrary LTI model `SYS` to transfer function format. The output `TFSYS` is a TF object.

`TFSYS = TF(SYS,'inv')` uses a fast algorithm for state-space `SYS`, but is typically less accurate for high-order systems.

You can create SISO or MIMO transfer functions (TF) by

`SYS = TF(NUM,DEN)` Continuous-time system `NUM(s)/DEN(s)`

`SYS = TF(NUM,DEN,T)` Discrete-time system `NUM(z)/DEN(z)` with sampling time `T` (Set `T=-1` if undetermined)

`SYS = TF` Default empty TF object

`SYS = TF(M)` Static gain matrix

`SYS = TF(NUM,DEN,LTI)` Transfer function with LTI properties inherited from system `LTI` (can be SS, TF, or ZPK).

All the above syntaxes may be followed by Property/Value pairs.

(Type "help Itiprops" for details on assignable properties).

The output `SYS` is a TF object.

The default TF variables 's' and 'z' can be altered by resetting the 'Variable' property. Alternatives include 'p' for continuous TF and 'z^-1' or 'q' for discrete TF.

For SISO systems, `NUM` and `DEN` are row vectors listing the numerator and denominator coefficients in

- \* descending powers of s or z by default
- \* ascending powers of q =  $z^{-1}$  if 'Variable' is set to ' $z^{-1}$ ' or 'q' (DSP convention).

For MIMO systems with NU inputs and NY outputs, NUM and DEN are NY-by-NU cell arrays of row vectors where NUM{i,j} and DEN{i,j} specify the transfer function from input j to output i. For example,

tf( {-5 ; [1 -5 6]} , {[1 -1] ; [1 1 0]})  
specifies the two-output/one-input system

$$\begin{bmatrix} -5/(s-1) & \\ (s^2-5s+6)/(s^2+s) & \end{bmatrix}$$

**ZPK** Specify zero-pole-gain models or convert to zero-pole-gain form.

ZSYS = ZPK(SYS) converts an arbitrary LTI model SYS to zero-pole-gain form. The output ZSYS is a ZPK object.

ZSYS = ZPK(SYS,'inv') uses a fast algorithm for state-space SYS, but is typically less accurate for high-order systems with low gain at  $s=0$ .

You can create SISO or MIMO zero-pole-gain (ZPK) models by:

SYS = ZPK(Z,P,K) Continuous-time system.

SYS = ZPK(Z,P,K,T) Discrete-time system with sample time T  
(Set T=-1 if undetermined)

SYS = ZPK Default empty zero-pole-gain object

SYS = ZPK(M) Static gain matrix

SYS = ZPK(Z,P,K,LTI) ZPK model with LTI properties inherited from system LTI (can be SS, TF, or ZPK).

All the above syntaxes may be followed by Property/Value pairs (Type "help Itiprops" for details on assignable properties).

The output SYS is a ZPK object.

For SISO systems, Z and P are the vectors of zeros and poles (set to [] if none) and K is the scalar gain.

For MIMO systems with NU inputs and NY outputs,

- \* Z and P are NY-by-NU cellarrays where Z{i,j} and P{i,j} are the vectors of zeros and poles of the transfer function from input j to output i
- \* K is the 2-D matrix of gains for each I/O channel.

For example,

zpk( {[1];[2 3]} , {1;[0 -1]} , [-5;1] )  
specifies the one-input/two-output system

$$\begin{bmatrix} -5/(s-1) & \\ (s-2)(s-3)/s(s+1) & \end{bmatrix}$$

## NOTE: